Bottom Up Parsers

Bottom-Up Parsing

- Construct parse tree bottom-up, from leaves (tokens) to root S
- Always construct right-most derivation, but in reverse order
- Algorithms:

shift-reduce

LR parsing (LR(0), SLR, LR(k), LALR(k), ...)

Shift-Reduce Parsing

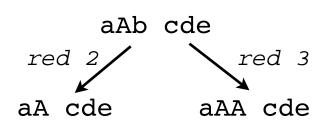
Shift-Reduce: look for substrings that match lhs of a production and *reduce* them by applying the production in reverse.

Grammar

Parsing as derivation in reverse

1)	s -	→	aAcBe	abbcde	shift	aAc de	shift
2)	A -	→	Ab	a bbcde	shift	aAc <u>d</u> e	red 4
3)	A -	→	b	a <u>b</u> bcde	red 3	аАсВ е	shift
4)	В -	→	d	aA bcde	shift	<u>aAcBe</u>	red 1
·				a <u>Ab</u> cde	red 2	S	
				aA cde	shift		

Ambiguity!



The underlined substrings are called **handles**.

Some terminology

A rightmost derivation is one where the rightmost nonterminal is replaced at each step. Write $\alpha \Rightarrow \beta$ for a rightmost derivation step.

$$s \Rightarrow^* \alpha Aw \Rightarrow \alpha \beta w \Rightarrow^* v$$
 (where $w, v \in T^*$)

Here β is a handle -- a substring that is the lhs of a production in a rightmost derivation (for v). If $s \Rightarrow \gamma$, then g is called a right sentential form.

The handles are the substrings that should be reduced in a shift-reduce parse.

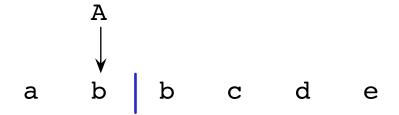
$$a\underline{\mathbf{Ab}}$$
 $cde \Leftarrow_2 aA cde \Leftarrow^* S$ $aA\underline{\mathbf{b}}$ $cde \Leftarrow_3 aAA cde$ not a handle

aAcde is a right sentential form, while aAAcde is not.

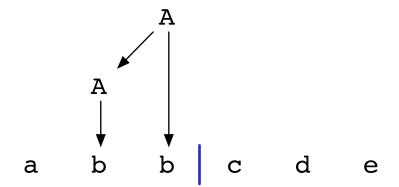
- 1) $S \rightarrow aAcBe$
- 2) $A \rightarrow Ab$
- 3) $A \rightarrow b$
- 4) $B \rightarrow d$

a b b c d e

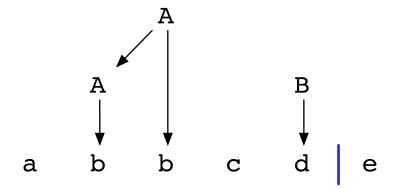
- 1) $S \rightarrow aAcBe$
- 2) $A \rightarrow Ab$
- 3) $A \rightarrow b$
- 4) $B \rightarrow d$



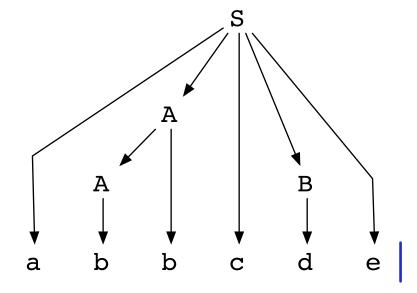
- 1) $S \rightarrow aAcBe$
- 2) $A \rightarrow Ab$
- 3) $A \rightarrow b$
- 4) $B \rightarrow d$



- 1) $S \rightarrow aAcBe$
- 2) $A \rightarrow Ab$
- 3) $A \rightarrow b$
- 4) $B \rightarrow d$



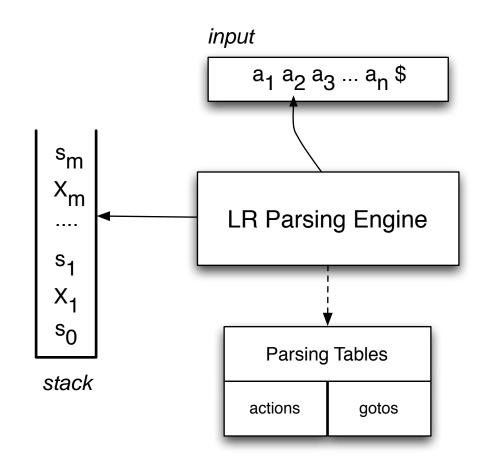
- 1) $S \rightarrow aAcBe$
- 2) $A \rightarrow Ab$
- 3) $A \rightarrow b$
- 4) $B \rightarrow d$



LR parsers

Problem: find the handles (and corresponding productions)

Solution: define a DFA that determines when to shift, when to reduce, when to accept, when to signal error



Advantages of LR Parsers

- LR parsers can handle virtually all programming language constructs expressible in context free grammars
- LR parsing is most general nonbacktracking shift-reduce parsing method, yet is efficiently implementable
- Class of grammars parsed by LR parsers is larger than that parsed by predictive parsers
- LS parsers can detect syntactic errors as soon as possible, given left to right scan of input

Building LR Parser Tables

Grammar

- 0) $S' \rightarrow S\$$
- 1) $S \rightarrow aAcBe$
- 2) $A \rightarrow Ab$
- 3) $A \rightarrow b$
- 4) $B \rightarrow d$

Items

```
S \rightarrow .aAcBe A \rightarrow .Ab B \rightarrow .d

S \rightarrow a.AcBe A \rightarrow A.b B \rightarrow d.

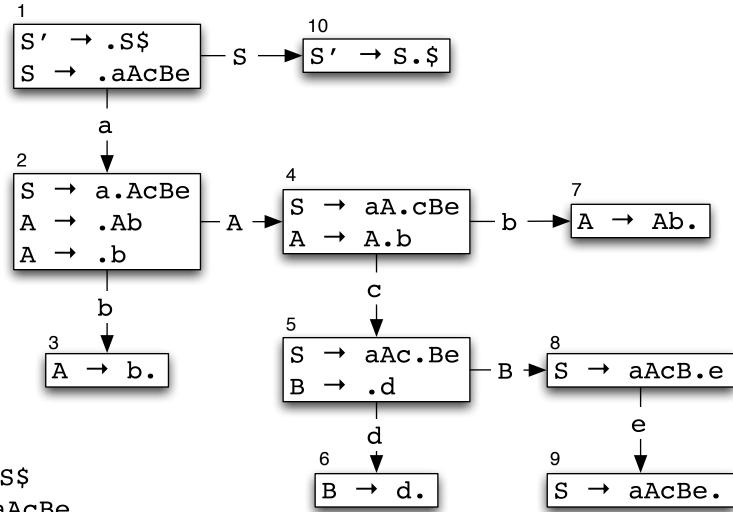
S \rightarrow aA.cBe A \rightarrow Ab.

S \rightarrow aAc.Be

S \rightarrow aAcB.e A \rightarrow .b S' \rightarrow .S$

S \rightarrow aAcBe. A \rightarrow b. S' \rightarrow .S$
```

Building LR Parser DFA



Grammar

- 0) $S' \rightarrow S$$
- 1) $S \rightarrow aAcBe$
- 2) $A \rightarrow Ab$
- 3) $A \rightarrow b$
- 4) $B \rightarrow d$

LR Parser Table

	a	b	С	d	е	\$	A	В	S
1	s2								10
2		s 3					4		
3	r3	r3	r3	r3	r3	r3			
4		s7	s 5						
5				s 6				8	
6	r4	r4	r4	r4	r4	r4			
7	r2	r2	r2	r2	r2	r2			
8					s9				
9	r1	r1	r1	r1	r1	r1			
10						!			